

the improbable yet elementary case

@causalmechanics/ @themanual4am

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a mathematical paradigmatic mashup: Thomas Kuhn Vs map-territory Vs ...?

*prefer the simplest explanation*¹

consider all mathematics as pseudo-mathematics; a means for a novice mathematician to express ideas in less time and fewer words than a similarly novice writer might, in prose. all terms are tentative. corrections \wedge advice, welcome.

...

¹which works

1 paradigm, measure, common measures, incommensurability

$$(Pa, Me, \overset{\cap}{Me}, \overset{\cap \emptyset}{Me})$$

1.1 a gentle introduction

$$(Pa, Me)$$

Let us consider a paradigm Pa , as a set of two measures Me_1 and Me_2 :

$$Pa = \{Me_1, Me_2\} : |Pa| = 2$$

1.2 totality, commonality

$$(\cup, \cap)$$

If paradigm Pa_1 , contains measures $Me_{1,2,3}$, and paradigm Pa_2 , contains measures $Me_{2,3,4}$:

$$Pa_1 = \{Me_1, Me_2, Me_3\}$$

$$Pa_2 = \{Me_2, Me_3, Me_4\}$$

The *set-of-all* measures $\overset{\cup}{Me}$, across Pa_1 and Pa_2 , can be found by union \cup :

$$\overset{\cup}{Me} = Pa_1 \cup Pa_2 = \{Me_1, Me_2, Me_3, Me_4\}$$

The *set-of-common* measures $\overset{\cap}{Me}$, between Pa_1 and Pa_2 , can be found by intersection \cap :

$$\overset{\cap}{Me} = Pa_1 \cap Pa_2 = \{Me_2, Me_3\}$$

Observing:

$$|\overset{\cup}{Me}| = 4, |\overset{\cap}{Me}| = 2, |\overset{\cap}{Me}| < |\overset{\cup}{Me}|$$

note: remember, this is a simplification, and an introduction

1.3 incommensurability

$$(\cap \emptyset)^2$$

Consider paradigms Pa_3 and Pa_4 , whereby:

$$Pa_3 = \{Me_1, Me_2, Me_3\}$$

$$Pa_4 = \{Me_4, Me_5, Me_6\}$$

When paradigms Pa_3 and Pa_4 , do not share common measures, then $\overset{\cap}{Me}$, is an empty set \emptyset :

$$\overset{\cap}{Me} = Pa_3 \cap Pa_4 = \emptyset : |\emptyset| = 0$$

And paradigms Pa_3 and Pa_4 , can be said to be incommensurable $\overset{\cap \emptyset}{Me}$:

$$\overset{\cap}{Me} = Pa_3 \cap Pa_4 = \emptyset : \overset{\cap}{Me} \rightarrow \overset{\cap \emptyset}{Me}, |\overset{\cap \emptyset}{Me}| = 0$$

□

²famously, two paradigms which share no common measures are incommensurable.